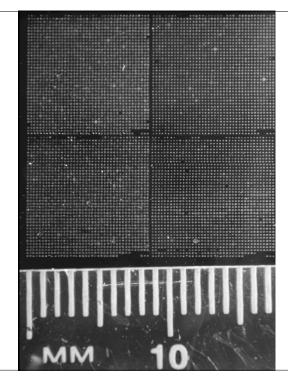
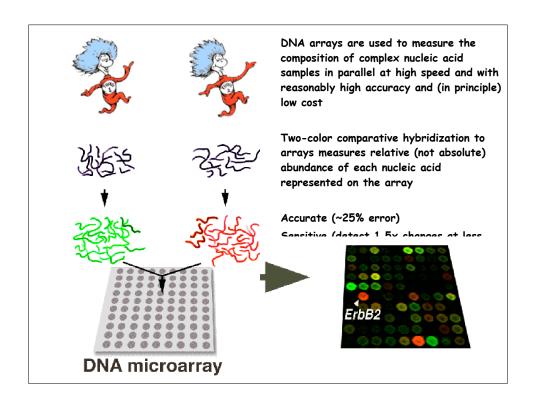
```
0.07 0.496 0.432 1.682 0.195 0.15 0.314
           0.18 -1.45 0.581 -0.296 -1.45
          -0.1 - 0.192 \quad -0.11 \quad -0.38 \quad 0.817 \quad 0.038 \quad 0.284 \quad 0.983 \quad -0.1 - 0.192 \quad -0.11 \quad -0.38 \quad 0.817 \quad 0.038 \quad 0.284 \quad 0.983 \quad -0.192 \quad -0.11 \quad -0.192 \quad -0.11
 -0.247 \quad 0.137 \quad -0.34 \quad 0.31 \quad 0.695 \quad 0.591 \quad 1.547 \quad 0.186 \quad -0.247 \quad 0.137 \quad -0.34 \quad 0.31 \quad 0.695 \quad 0.591 \quad 1.547 \quad 0.186 \quad -0.247 \quad 0.187 \quad -0.34 \quad 0.31 \quad 0.695 \quad 0.591 \quad 0.59
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  0.358 -0.649
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^{0.15}_{-0.124} ^{-0.405}_{-0.44} The practical art of analyzing whole-genome ^{1.49}_{-0.07} ^{1.025}_{1.983}
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-2.158
                                                                                                                                                  (using spotted DNA microarrays)
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-0.192 -0.1
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  -0.34 0.591
0.29 0.389 Audrey P. Gasch, PhD -0.247 0.31 -0.34 0.591 0.695 0.186
0.358 -0.44 0.29 0.389 0.581 0.494
 -0.649 0.358 -0.44
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                                                                                                                                                                                                                               Mike Eisen lab
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                                                                                          0.38
                                                                                                                                           0.23 0.149 Lawrence Berkeley Lab 0.15 0.29 0.23 0.149
 -0.005 0.15 0.29
     -0.44 -0.124 -0.25 0.05 0.007 0.195 -0.44 1.983 -0.44 -0.124 -0.25 0.05 0.007 0.195 -0.44 1.983
     0.15 \quad 0.314 \quad 0.77 \quad 0.07 \quad 0.496 \quad 0.432 \quad 1.682 \quad 0.195 \quad 0.15 \quad 0.314 \quad 0.77 \quad 0.07 \quad 0.496 \quad 0.432 \quad 1.682 \quad 0.195 \quad 0.
     -1.141 -0.287 -0.97 -0.08 0.011 -0.222 1.737 -0.38 -1.141 -0.287 -0.97 -0.08 0.011 -0.222 1.737
        -0.1 \ -0.192 \quad -0.11 \quad -0.38 \quad 0.817 \quad 0.038 \quad 0.284 \quad 0.983 \qquad -0.1 \ -0.192 \quad -0.11 \quad -0.38 \quad 0.817 \quad 0.038 \quad 0.284
0.247 \quad 0.137 \quad -0.34 \quad 0.31 \quad 0.695 \quad 0.591 \quad 1.547 \quad 0.186 \quad -0.247 \quad 0.137 \quad -0.34 \quad 0.31 \quad 0.695 \quad 0.591 \quad 1.547 \quad 0.186 \quad 0.591 \quad 0.591
0.358 -0.649 0.29 -0.44 0.581 0.389 0.916 0.494 0.358 -0.649 0.29 -0.44 0.581 0.389 0.916
0.38 0.305 1.296 1.658
     0.15 -0.005 0.23
                                                                                                                                        -0.25 0.195 0.007 1.983 -0.44 -0.124 -0.44 0.05
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              -0.25 0.195
```



# Spotted DNA Arrays

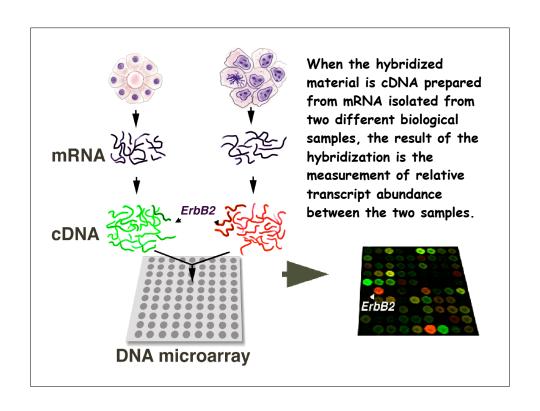
Pre-synthesized DNA (e.g. from PCR or oligo synthesis)

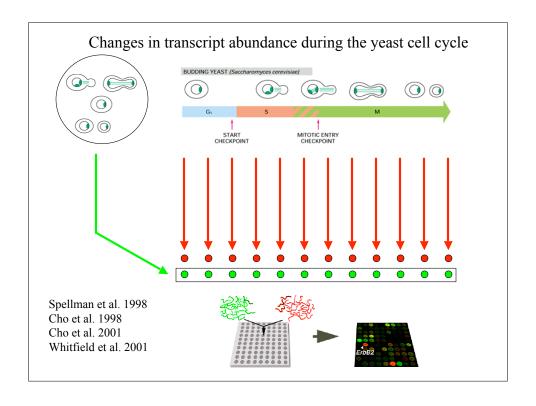
Robotically deposited on treated glass microscope slides in regular array

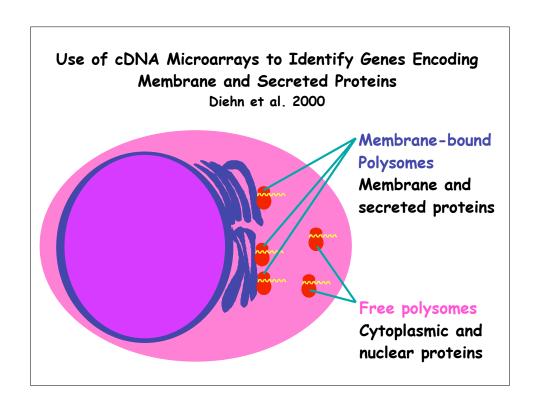


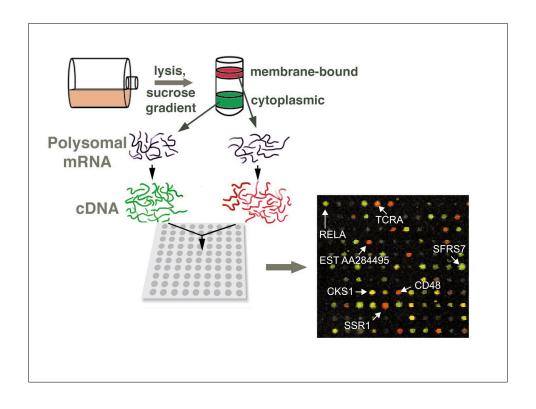
# Microarrays can be used for any procedure that can take advantage of complementary DNA hybridization

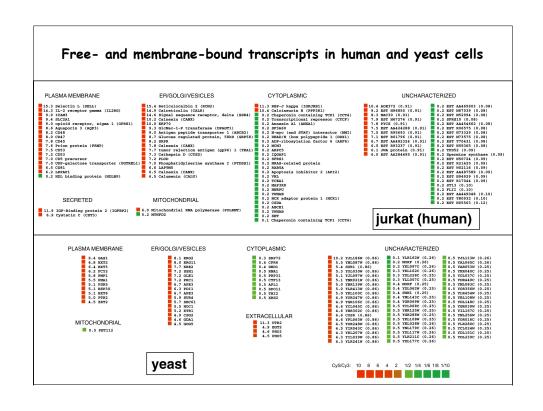
- Gene expression analysis
- RNA localization
- RNA turnover
- RNA splicing and processing
- KINA splicing and processing
- Genotyping/Karyotyping
- Population analysis
- Population genomics
- Diagnostics/classification
- Chromatin & RNA immunoprecipitation

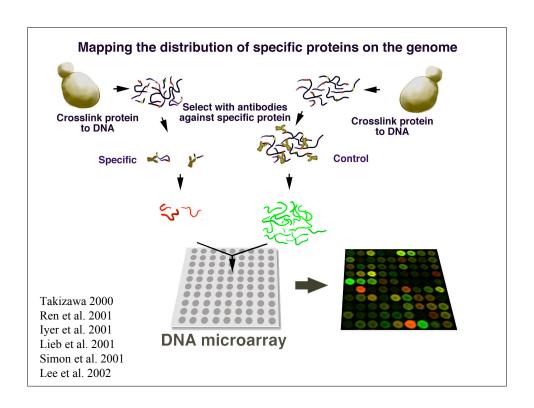


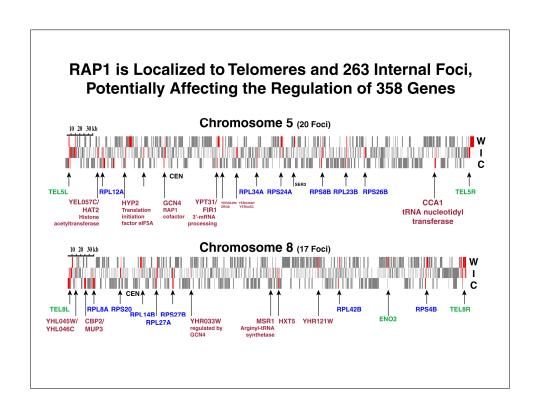


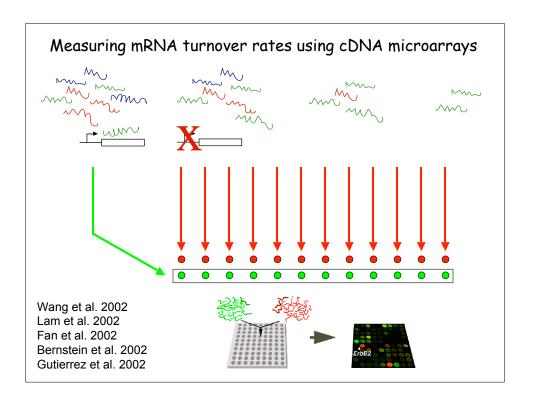


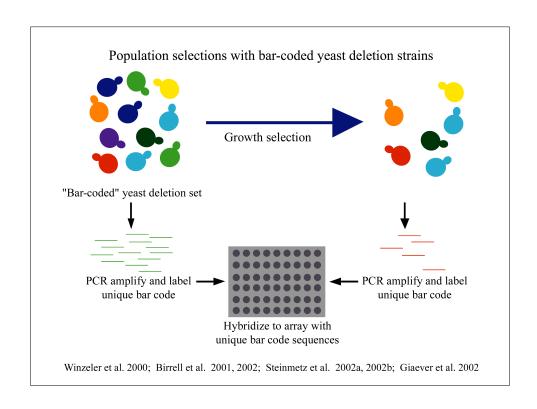


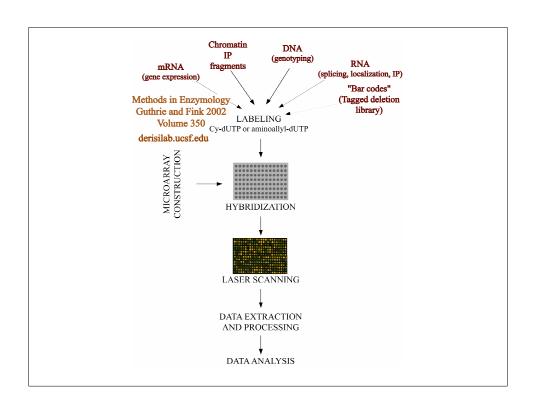


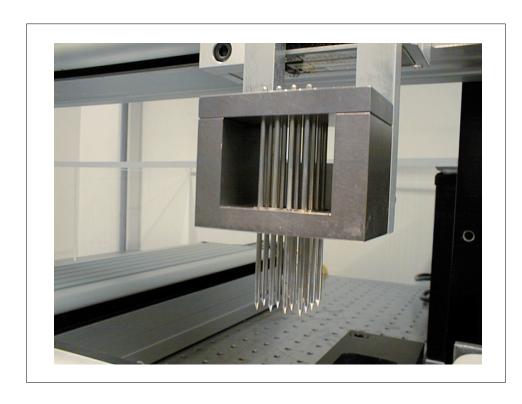


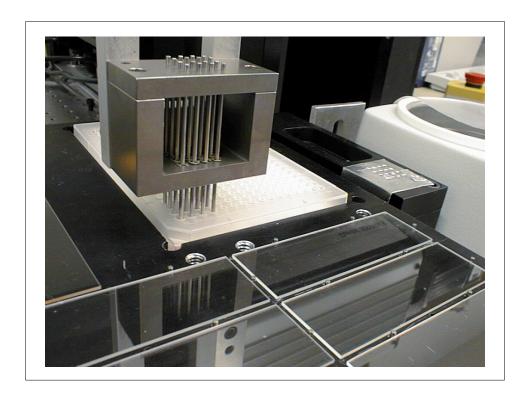


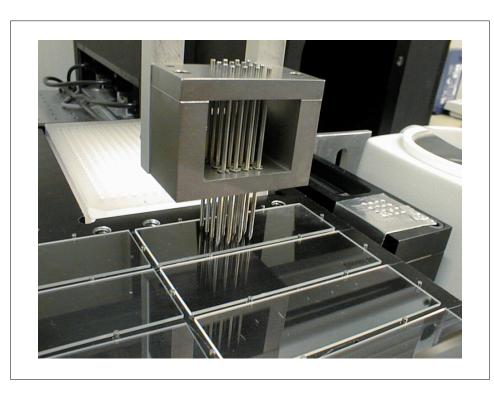


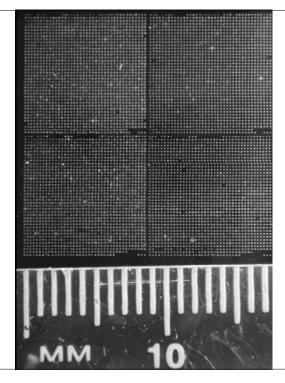








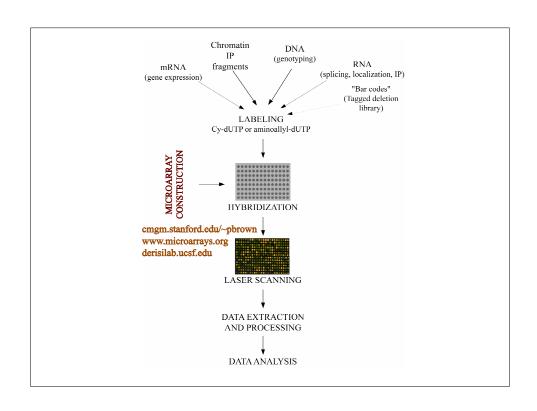


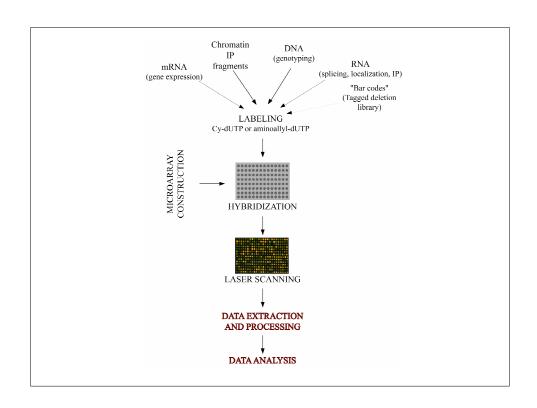


# Spotted DNA Arrays

Spots can now be printed with center to center spacing of less than 100um, allowing for more than 150,000 spots to be printed on a standard glass slide.

A good robot can now print 50,000 spots on 200 slides in 24





### Microarray hybridization design: which samples to compare?

Only requirement: good signal in reference channel

- 1. Directly compare two samples
  - -- Tissue A vs. Tissue B
  - -- Timepoint 60 min vs. Timepoint 0
- 2. Compare one sample to pool of samples
  - -- Tissue A vs. pool of all tissues
  - -- Timepoint 60 min vs. pool of timepoints
- 3. Compare each sample to genomic DNA
- 4. Loop design: successive comparisons
  - -- S1 vs S2 S2 vs S3 S3 vs S4 S5 vs S6 S6 vs S1

### Deconvoluting microarray data: ratios of ratios

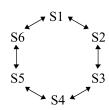
Eg. Timecourse of mRNA samples vs. genomic DNA

Array 1: 
$$\frac{\text{mRNA (t = 0 min)}}{\text{genomic DNA}}$$
 Array 2:  $\frac{\text{mRNA (t = 60 min)}}{\text{genomic DNA}}$ 

$$\frac{\text{Array 1}}{\text{Array 2}} = \frac{\frac{\text{mRNA (t = 60 min)}}{\text{genomic DNA}}}{\frac{\text{mRNA (t = 0 min)}}{\text{genomic DNA}}} = \frac{\text{mRNA (t = 60 min)}}{\text{mRNA (t = 0 min)}}$$

### Deconvoluting microarray data: ratios of ratios

Eg. Loop design: successive comparisons S1 vs S2 S2 vs S3 S3 vs S4 S5 vs S6 S6 vs S1



#### Drawbacks:

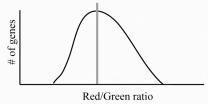
-- Need to do lots of deconvolutions to extract direct comparison information:

Therefore missing data on one array = missing data on ALL of the arrays and error gets distributed during deconvolutions

## NORMALIZATION METHODS

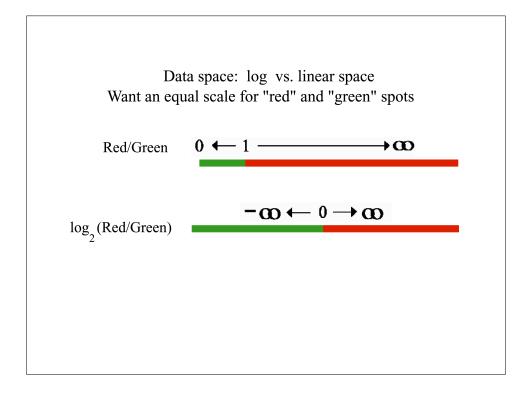
1. Assumption: average gene will not change in expression:

adjust one channel intensity such that average gene expression change R/G = 1



- 2. Normalization by cell number (not RNA mass)
- 3. Dope labeling reactions with controls of known abundance with corresponding target spotted onto microarrays
- 4. Regional normalization across microarray

(Terry Speed method) Yang et al. 2002 NAR



### Data selection:

- Ideally based on experimental reproducibility
  - -- t-test (with Bonferroni multiple-test correction)
  - -- SAM package (Tusher et al. 2001; R. Tibsharani website)
  - -- ANOVA
- Often based on arbitrary cutoffs
  - -- transcripts that change > arbitrary fold-cutoff
  - -- transcripts that change >cutoff in arbitrary # of experiments

Always do initial control experiments to define your own variability

### How many replicates??

Answer: depends on the desired confidence (and personal reproducibility)

Should do a minimum of 2-3 replicates for simple expression experiments

- -- can get increased confidence in timecourse experiments (nonrandom patterns of gene expression over time)
- -- can get increased confidence in functionally-related genes (eg. 135 ribosomal proteins acting in concert)

Based on the initial variance can do additional replicates if desired

Observation in many different organisms:

Genes that encode functionally related proteins are often coexpressed at the level of transcript abundance

Therefore, a common goal in gene expression analysis is to identify similarly expressed genes

First step in doing this: choose a similarity metric

#### **SIMILARITY METRIC:**

gene expression pattern = n-dimentional vector

## Euclidean distance: shortest distance

shortest distance between two points



# Pearson correlation (cosine-angle distance):

angle between two vectors (ie the direction they point)



Expression change change

Time

These patterns would be correlated using Pearson correlation but not Euclidean distance

\*\* Using the WEIGHTED Pearson correlation is very useful for large datasets (to underweight highly similar experiments)

#### COMPUTATIONAL METHODS OF ANALYSIS

Excellent review by J. Quakenbush 2001 *Nature Reviews-Genetics*Nearest neighbors of a query gene

Clustering: grouping similarly expressed genes together

- -- Hierarchical clustering
- -- Self Organizing Maps (SOMs)
- -- K-means clustering

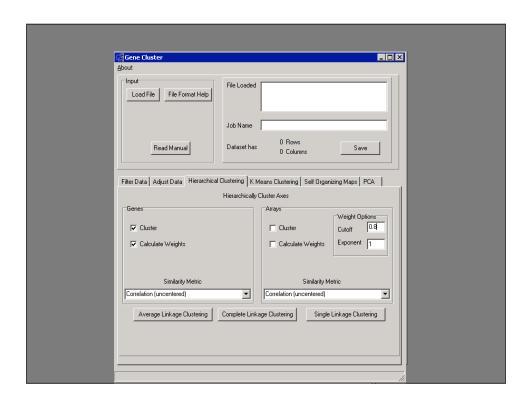
#### More complicated algorithms:

- -- Support Vector Machines (SVMs)
- -- Principal Component Analysis (PCA = SVD)
- -- Bayesian Networks
- -- all kinds of heuristic algorithms

_	en's Cluster software: available at http://rana.lbl.gov
	About Input I File Format Help  Job Name  Dataset has 0 Rows 0 Columns  Save
	Filter Data   Adjust Data   Hierarchical Clustering   K Means Clustering   Self Organizing Maps   PCA    Filter Genes
Also	other commercially-available software: Genespring, Spotfire

© Gene Cluster□ X
Load File   File Format Help   Job Name
Read Manual Dataset has 0 Rows 0 Columns Save
Log Transform Data  Normalize  Arrays  Order of Operations:  Uog Transform  Order of Operations:  Uog Transform  Center Genes  Median Center  Arrays  Arrays  Mean Center  Arrays  Arrays
Arrays Normalize Genes Center Arrays Normalize Arrays

Gene Cluster  About	×
Input Load File File Format Help	File Loaded results\Extrastress\bootstrap\11boot0_0_finalProt otypes.bt
	Job Name 11boot0_0_finalPrototypes
Read Manual	Dataset has 104 Columns Save
Filter Data   Adjust Data   Hierarchica	al Clustering   K Means Clustering   Self Organizing Maps   PCA
Genes	Hierarchically Cluster Axes
	☐ Cluster ☐ Calculate Weights
Similarity Metric  [Correlation (uncentered)	Similarity Metric  Correlation (uncertered)
Average Linkage Clustering	Complete Linkage Clustering Single Linkage Clustering
Done Loading Data	



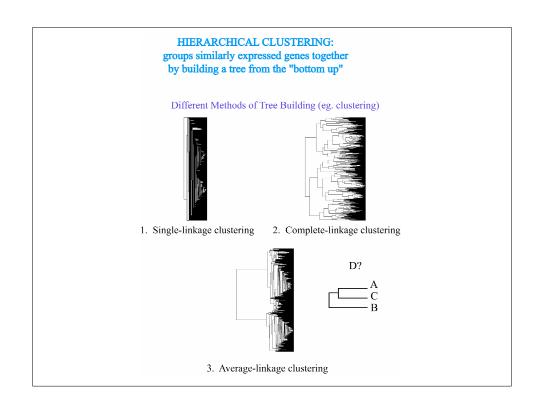
# Gene and Array weighting for clustering analysis as described in Cluster manual (rana.lbl.gov)

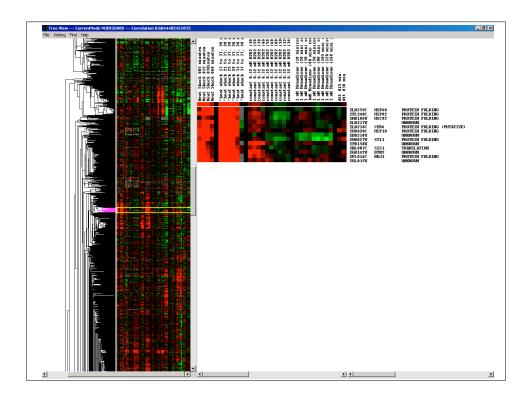
$$\begin{split} L_{\dot{1}} = & \sum_{\substack{\text{overall all rows j} \\ \text{where } d < \text{cutoff}}} \frac{\left(\text{cutoff - dist(i,j)}\right)^n}{\text{cutoff}} \qquad & W_{\dot{i}} = \underbrace{1}_{\dot{i}} \end{split}$$

If two arrays are identical, their corr = 1 and distance = 1-corr = 0

For exponent 
$$n = 1$$

$$L = (0.2 - 0) + (0.2 - 0) = 2$$
  $W = 0.5$ 





# Many people are initially overwhelmed with the massive volume of data

### Tips for initial data exploration

- 1. Make a first pass through the data, looking at thumbnail image, to an overview of the global gene expression programs
- 2. Next, go back through the data, cluster by cluster
  - -- digest the gene expression pattern of each cluster
  - -- glance at the genes in the cluster and look for relationships (functional, regulatory, etc)
- 3. Finally, go through the data in detail and focus on individual genes and small groups of genes

### A useful function: the hypergeometric distribution

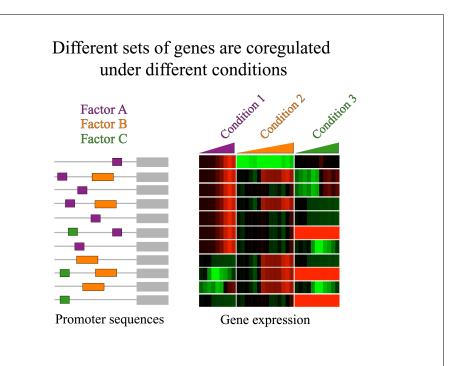
Can calculate the probability of observing at least q related objects in a cluster of l objects, based on the total number of related objects (M) in the genome of N genes.

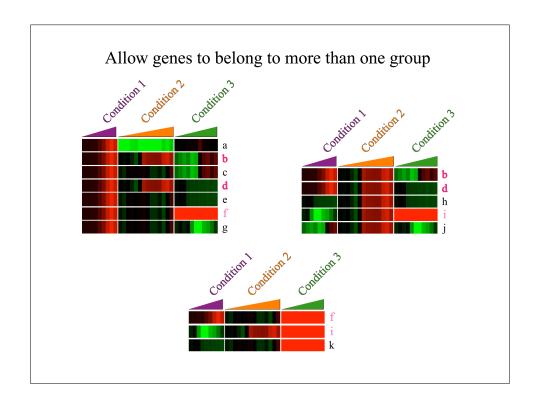
$$P = \sum_{i=q}^{l} \frac{\binom{M}{i} \binom{N-M}{l-i}}{\binom{N}{l}}$$

Example: Probability of observing 8 protein folding chaperones in a cluster of 15 genes, when there are 20 chaperones in a genome of 6,000 genes

$$P = \sum_{i=q}^{l} \frac{\binom{20}{i} \binom{6000 - 20}{15 - i}}{\binom{6000}{15}} = 2 \times 10^{-17}$$

8/15 chaperones in cluster = 53% 20/6000 chaperones in genome = 3% = 18-fold enrichment in cluster





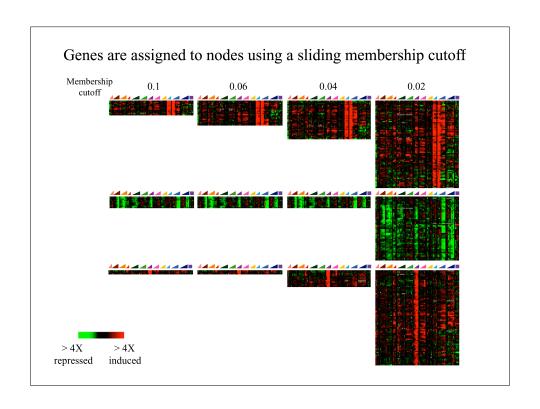
### Modified Fuzzy k-means clustering

Based on the method developed by Bezdek *et al.* c. 1980 Heuristically modified to analyze yeast genomic expression data

### Algorithm output:

- A list of cluster nodes (represented by average expression patterns)
  - A matrix of each gene's membership to each cluster node

Genes are assigned to each cluster to which they are similar above a user-defined membership cutoff



*FuzzyK* is a C++ command line program that runs on Linux

The results can be viewed with the PERL program *FuzzyExplorer* 

Both are available at http://rana.lbl.gov/FuzzyK

### Final words about microarray data analysis

- 1. While analyzing data, always be aware of:
  - -- exact features of the experiment
  - -- normalization method
- 2. Be careful about gene annotations:
  - -- often limited
  - -- sometimes incorrect
  - -- many genes have multiple functions that are hard to capture
- 3. Remember that cells may experience the experimental conditions beyond your interpretation ...
  - -- be aware of pleiotropic conditions
  - -- be aware of secondary effects of conditions
- 4. The power of comparison: many responses may not be specific to your conditions